Level 1 / Level 2 GCSE (9-1)

## MATHEMATICS

Paper 1 (Non- calculator)
Higher Tier
Time : $\mathbf{1}$ hour 30 minutes
Paper : 1 MA1 / 1H

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.

- You must show all your working.
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- Calculators may not be used.


## Information

- The total mark for this paper is 80.
- The marks for each question are shown in brackets - use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

Answer ALL questions.

## Write your answers in the spaces provided.

## You must write down all the stages in your working.

1. There are only red discs, blue discs, white discs and black discs in a box.

The table shows the probability of taking at random a red disc from the box.

| Colour | Red | Blue | White | Black |
| :--- | :--- | :--- | :--- | :--- |
| Probability | 0.1 |  |  |  |

The number of black discs in the box is the same as the number of red discs in the box.
The number of white discs in the box is three times the number of blue discs in the box.
a. Complete the table

There are 8 red discs in the box.
b. Work out the total number of discs in the box.
2. A person on holiday in the North Macedonia changed $480 \in$ into Macedonian denar when the exchange rate was $1 \mathrm{MKD}=0.016$ Euros. His total expenses were 3500 MKD per night for the three nights. And his other expenses were 8000 MKD for meal, 2275 MKD for travel costs. On returning home he changed what denar he had left into euro at a rate of 61.5 MKD = 1 Euro

## Calculate

a. the number of denars received for the $480 \in$.
b. The total amount spent, in denars.
c. the amount in euros obtained for the denars he had left.
3. Find the lowest common multiple (LCM) of 30 and 48.
4. Here is the plan, front elevation and side elevation views of a prism, drawn on cm squared paper.


In the space below, draw a sketch of the solid shape. Give the dimensions of the solid on your sketch.
5.

a. Reflect triangle $\mathbf{A}$ in the line $y=x$. Label the image $\mathbf{B}$.
b. Describe fully the single transformation that maps $\mathbf{C}$ onto $\mathbf{A}$.
$\qquad$
$\qquad$
6. $£ 1800$ is raised and divided among 3 charities $P, Q, R$ in the proportion $3: 5: 7$.
a. Find the amount each charity receives.
b. If these amounts are represented on a pie chart, calculate the angle of each sector.
7. Here is a diagram of a square and a rectangle.

$K L=8 \mathrm{~cm}$
The perimeter of a square is 48 cm .
The area of $K L M N$ is the same as the area of $A B C D$. Find the length of $L M$.
8. a. Work out an estimate of the value of $(13.2 \times(7.1-4.9))^{2}$
b. Find the value of $16^{-\frac{1}{2}}$
c. The Nile is the longest river in Africa, which has a length of about 6758 km . Write the length correct to 1 significant figure.
km
9. Work out $3 \frac{3}{8} \div 1 \frac{1}{6}$

Give your answer as a mixed number in its simplest form.
10.


The diagram shows two straight lines.
The equation of the lines are $y=x+1$ and $3 x+2 y=12$.
a. Write down the solutions of the simultaneous equations.

$$
\begin{array}{r}
y=x+1 \\
3 x+2 y=12
\end{array}
$$

b. Find an equation of the line which is perpendicular to the line with equation $3 x+2 y=12$ and passes through the point $(0,9)$.
11. There are 11 players in a football team A .

Here are the ages, in years, of these players.

| 20 | 25 | 17 | 28 | 19 | 25 | 24 | 18 | 27 | 22 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

a. i. Find the interquartile range of these ages.
ii. Find the median of these ages.

Here is the information about the ages, of the 11 players in a football team B.

| Median | 26 |
| :---: | :---: |
| Lower quartile | 20 |
| Upper quartile | 31 |
| Least age | 19 |
| Greatest age | 35 |

Use the information above to compare the ages of football team A and team B.
Write down two comparisons.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
12. Here are the three squares


A


B


C

The area of square B is $40 \%$ more than the area of square A .
The area of square C is $60 \%$ more than the area of square B .

Find the area of square A as a fraction of the area of square C .
13. Given that $n$ can be any integer such that $n>1$, prove that $n+n^{2}$ is never an odd number.
14.


Triangle $A B C$ is right-angled at $B$.
$B C=2 \sqrt{3} \mathrm{~cm}$ and $C=30^{0}$
Work out the length of $A B$.
15. Given that $6 x^{2}-13 x-5=0$

Find the possible values of $x$.
16. The diagram shows a solid shape made from a hemisphere and a cone.


The hemisphere and a cone both have a radius of 3 cm .
The total height of the solid shape is 12 cm .
Calculate the volume of the solid, in terms of $\pi$.
17. Express $\frac{(2 \sqrt{3})^{2}}{6-3 \sqrt{3}}$ in the form $p(q+\sqrt{3})$ where $p$ and $q$ are integers.
18. Given that $x^{2}+8 x+10=(x+a)^{2}+b$ for all values of $x$,
a. find the value of $a$ and the value of $b$.
$\qquad$
b. Write down the minimum value of the expression $x^{2}+8 x+10$
$\qquad$
c. Write down the equation of the line of symmetry of the graph of $y=x^{2}+8 x+10$
19. $F$ is directly proportional to $d^{2}$
$H$ is inversely proportional to $F$
Given that $H=10$ and $d=2$ when $F=20$
Find a formula for $H$ in terms of $d$.
20. Given the function
$\mathrm{f}(x)=2 x-1$ and $\mathrm{g}(x)=x^{2}$
Show that equation $\mathrm{f}^{-1}(x)=\operatorname{gf}(x)$ is $8 x^{2}-9 x+1=0$
21. There are only red discs and black discs in a bag.

There are two less red discs than black discs in a bag.
The probability that Arthur will take two discs of different colour is $\frac{15}{28}$.
Work out the number of black discs in the bag.

